

問

次の行列 A の逆行列を求めよ。

$$A = \begin{bmatrix} 3 & 3 & -5 & -6 \\ 1 & 2 & -3 & -1 \\ 2 & 3 & -5 & -3 \\ -1 & 0 & 2 & 2 \end{bmatrix} .$$

$$A^{-1} = \begin{bmatrix} 4 & \boxed{(1)} & \boxed{(2)} & -3 \\ 0 & -1 & 1 & 1 \\ 1 & 3 & -3 & 0 \\ 1 & 6 & -5 & -1 \end{bmatrix}$$

$\boxed{(1)} = 18$

$\boxed{(2)} = -16$

3	3	-5	-6	1			
1	2	-3	-1		1		
2	3	-5	-3			1	
-1	0	2	2				1

① + 3 × ④
 ↓ ② + ④, ③ + 2 × ④

0	3	1	0	1	0	0	3
0	2	-1	1	0	1	0	1
0	3	-1	1	0	0	1	2
-1	0	2	2	0	0	0	1

↓ ① - ③
 ② - ③

0	0	2	-1	1	0	-1	1
0	-1	0	0	0	1	-1	-1
0	3	-1	1	0	0	1	2
-1	0	2	2	0	0	0	1

↓ ③ + 3 × ②

0	0	2	-1	1	0	-1	1
0	-1	0	0	0	1	-1	-1
0	0	-1	1	0	3	-2	-1
-1	0	2	2	0	0	0	1

1	0	0	0	4	18	-16	-3
0	1	0	0	0	-1	1	1
0	0	1	0	1	3	-3	0
0	0	0	1	1	6	-5	-1

↑

0	0	1	0	1	3	-3	0
0	1	0	0	0	-1	1	1
0	0	0	1	1	6	-5	-1
1	0	0	0	4	18	-16	-3

↑ ④ + 2 × ① + 2 × ③

0	0	1	0	1	3	-3	0
0	1	0	0	0	-1	1	1
0	0	0	1	1	6	-5	-1
1	0	-2	-2	0	0	0	-1

↑ ③ + ①
 (-1) × ④

0	0	1	0	1	3	-3	0
0	1	0	0	0	-1	1	1
0	0	-1	1	0	3	-2	-1
-1	0	2	2	0	0	0	1



① + ③
 (-1) × ②